

Write the following quadratic functions in standard form.  $y = a(x-h)^2 + k$

$a = -3$

1.  $f(x) = -3x^2 - 6x + 2$

$h = \frac{6}{2(-3)} = \frac{6}{-6} = -1$

$k = -3(-1)^2 - 6(-1) + 2 = 5$

$f(x) = -3(x+1)^2 + 5$

2.  $f(x) = \frac{1}{2}x^2 + 8x - 3$   $a = \frac{1}{2}$

$h = \frac{-8}{2 \cdot \frac{1}{2}} = \frac{-8}{1} = -8$

$k = \frac{1}{2}(-8)^2 + 8(-8) - 3 = -35$

$f(x) = \frac{1}{2}(x+8)^2 - 35$

3.  $f(x) = 4x^2 - 24x - 15$   $a = 4$

$h = \frac{24}{2 \cdot 4} = \frac{24}{8} = 3$

$k = 4(3)^2 - 24(3) - 15 = -51$

$f(x) = 4(x-3)^2 - 51$

4.  $f(x) = x^2 - 7x + 2$

$a = 1$   
 $h = \frac{7}{2 \cdot 1} = \frac{7}{2}$

$k = (\frac{7}{2})^2 - 7(\frac{7}{2}) + 2 = -\frac{41}{4}$

$f(x) = (x - \frac{7}{2})^2 - \frac{41}{4}$

Evaluate each polynomial for the given value of x using synthetic division. Show your work.

5.  $f(x) = x^4 - 5x^3 + 5x^2 + 5x - 6$

$f(-2) = \boxed{60}$

-2	1	-5	5	5	-6
	-2	14	-38	66	
	1	-7	19	-33	60

6.  $f(x) = x^3 - 2x^2 - 5x + 6$

$f(-6) = \boxed{-252}$

-6	1	-2	-5	6
	-6	48	-58	
	1	-8	43	-252

Find the quotient and the remainder. Determine if the binomial is a factor of the first polynomial.

7.  $f(x) = x^3 - 12x + 16 \div (x-2)$

2	1	0	-12	16
	2	4	-16	
	1	2	-8	0

$Q(x) = x^2 + 2x - 8$

$R(x) = 0$  YES

8.  $f(x) = x^3 + x^2 + x + 3 \div (x+1)$

-1	1	1	1	3
	-1	0	-1	
	1	0	2	

$Q(x) = x^2 + 1$

$R(x) = 2$  No

Express each function as a product of linear factors.

9.  $f(x) = x^3 + 6x^2 - x - 6$

1	1	6	-1	-6
1	7	6	0	
	-6	-6	-6	
	1	0	0	

$x^2 + 7x + 6$   
 $(x+6)(x+1)$

$f(x) = (x+6)(x+1)(x-1)$

10.  $f(x) = 2x^3 - 11x^2 - x + 30$

2	2	-11	-1	30
2	-7	-15	0	
	-9	-14	-15	
	2	-7	-15	

$2x^2 - 7x - 15$   
 $(2x+3)(x-5)$

$f(x) = (2x+3)(x-5)(x-2)$

Write the equation in factored form of a polynomial with the given roots.

11.  $3, \frac{1}{3}, -\frac{1}{2}$   
 $f(x) = (x-3)(3x-1)(2x+1)$

12.  $1 \pm 3i$   
 $f(x) = (x-1)^2(x-1+3i)(x-1-3i)$

List the possible rational roots.

13.  $f(x) = 2x^3 - 11x^2 - x + 30$   
 $\pm(1, 2, 3, 5, 6, 10, 15, 30, \frac{1}{2}, \frac{3}{2}, \frac{5}{2}, \frac{15}{2})$

14.  $f(x) = x^3 + 6x^2 - x - 6$   
 $\pm(1, 2, 3, 6)$

Find the exact zeros of each polynomial below. Use synthetic division when necessary.

15.  $f(x) = x^3 - 4x^2 + 9x - 10$   
 $\begin{array}{r|rrrr} 2 & 1 & -4 & 9 & -10 \\ & & 2 & -2 & 5 \\ \hline & 1 & -2 & 5 & 0 \end{array}$   
 $x^2 - 2x + 5 = 0$   
 $x = \frac{2 \pm \sqrt{2^2 - 4 \cdot 1 \cdot 5}}{2 \cdot 1} = \frac{2 \pm \sqrt{-16}}{2} = \frac{2 \pm 4i}{2} = 1 \pm 2i$

16.  $f(x) = x^3 - 4x^2 + 2x + 1$   
 $\begin{array}{r|rrrr} 1 & 1 & -4 & 2 & 1 \\ & & -4 & -2 & -1 \\ \hline & 1 & -3 & -1 & 0 \end{array}$   
 $x^2 - 3x - 1 = 0$   
 $x = \frac{3 \pm \sqrt{3^2 - 4 \cdot 1 \cdot (-1)}}{2 \cdot 1} = \frac{3 \pm \sqrt{13}}{2}$

17.  $f(x) = x^3 - 17x^2 + 70x - 54$   
 $\begin{array}{r|rrrr} 1 & 1 & -17 & 70 & -54 \\ & & -16 & 54 & 0 \\ \hline & 1 & -16 & 54 & 0 \end{array}$   
 $x^2 - 16x + 54 = 0$   
 $x = \frac{16 \pm \sqrt{16^2 - 4 \cdot 1 \cdot 54}}{2} = \frac{16 \pm \sqrt{40}}{2} = \frac{16 \pm 2\sqrt{10}}{2} = 8 \pm \sqrt{10}$

18.  $f(x) = x^3 - 7x^2 + 11x + 3$   
 $\begin{array}{r|rrrr} 3 & 1 & -7 & 11 & 3 \\ & & -4 & -1 & 0 \\ \hline & 1 & -4 & -1 & 0 \end{array}$   
 $x^2 - 4x - 1 = 0$   
 $x = \frac{4 \pm \sqrt{4^2 - 4 \cdot 1 \cdot (-1)}}{2} = \frac{4 \pm \sqrt{20}}{2} = \frac{4 \pm 2\sqrt{5}}{2} = 2 \pm \sqrt{5}$

$\frac{256}{40}$   
 $\frac{-216}{40}$

Perform the indicated operation.

19.  $(5+2i) + (6-7i) = 11-5i$

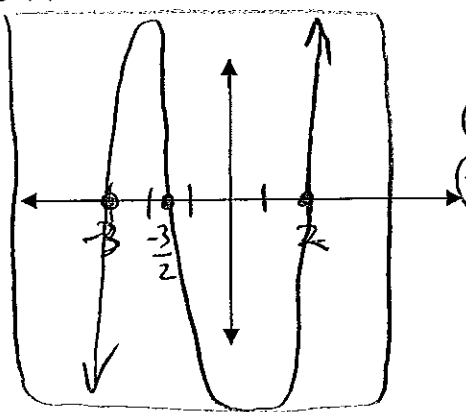
20.  $(8-3i) - (4+i) = 4-4i$

21.  $(1+3i)(2-5i)$   
 $2-5i+6i-15i^2 = 17+i$

22.  $\frac{3i}{1-4i} \cdot \frac{1+4i}{1+4i} = \frac{3i+12i^2}{1-16i^2} = \frac{-12+3i}{17}$   
 $-\frac{12}{17} + \frac{3}{17}i$

Find the (a) exact roots of the polynomial, (b) y-intercept, (c) number of actual relative extrema, then sketch the graph. (remember to label all the above on the graph)

23.  $f(x) = 2x^5 - 3x^4 - 19x^3 + 43x^2 + 27x - 90$

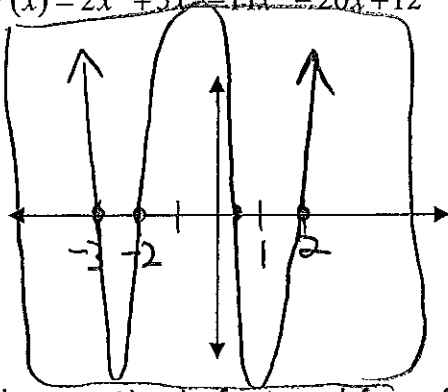


$\begin{array}{r|rrrrr} 2 & 2 & -3 & -19 & 43 & 27 & -90 \\ & & -6 & -25 & 11 & 54 & 0 \\ \hline 2 & 2 & -9 & -44 & 54 & 81 & -90 \\ & & 1 & -5 & -2 & 15 & 0 \\ \hline 2 & 2 & -8 & 10 & 0 & & \\ & & 2 & -4 & 5 & & \\ \hline & 2 & -4 & 5 & & & \\ & & 2 & -4 & 5 & & \\ & & & 4 & -4 & & \\ & & & & 4 & -4 & \\ & & & & & 2 & -2 \end{array}$   
 $x^2 - 4x + 5 = 0$   
 $x = \frac{4 \pm \sqrt{4^2 - 4 \cdot 1 \cdot 5}}{2} = \frac{4 \pm \sqrt{-4}}{2} = \frac{4 \pm 2i}{2} = 2 \pm i$

a)  $2, -3, -\frac{3}{2}, 2 \pm i$   
 b)  $(0, -90)$   
 c)  $4? 2$

24.

$$f(x) = 2x^4 + 5x^3 - 11x^2 - 20x + 12$$



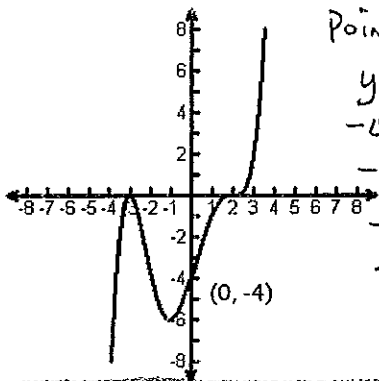
$$\begin{array}{r|rrrrr} 2 & 2 & 5 & -11 & -20 & 12 \\ \oplus & 2 & 9 & 7 & -6 & 0 \\ \ominus & 2 & 5 & -3 & 0 & \\ \hline & 2x^2 + 5x - 3 & = & 0 & & \\ & (2x-1)(x+3) & = & 0 & & \\ & \frac{1}{2}, -3 & & & & \end{array}$$

a)  $\frac{2, -2, \frac{1}{2}, -3}{}$

b)  $\frac{(0, 12)}{}$

c)  $\frac{3}{}$

Write the equation in factored form for the polynomials graphed below. Be sure to calculate the "a" value for the polynomial. Leave in factored form



Roots:  $-3(2), 2(3)$

Point:  $(0, -4)$

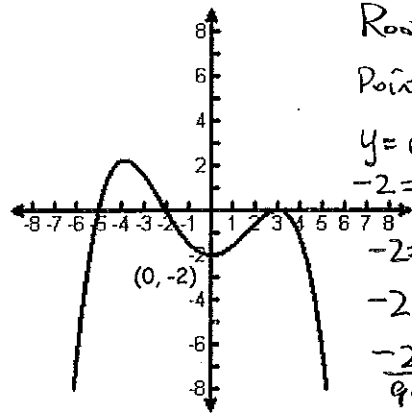
$$y = a(x+3)^2(x-2)^3$$

$$-4 = a(0+3)^2(0-2)^3$$

$$-4 = a \cdot 9 \cdot -8$$

$$-4 = a \cdot -72$$

$$\frac{-4}{-72} = a = \frac{1}{18}$$



Roots:  $-5, -2, 3(2)$

Point:  $(0, -2)$

$$y = a(x+5)(x+2)(x-3)^2$$

$$-2 = a(0+5)(0+2)(0-3)^2$$

$$-2 = a \cdot 5 \cdot 2 \cdot 9$$

$$-2 = a \cdot 90$$

$$\frac{-2}{90} = a = -\frac{1}{45}$$

25.

$$y = \frac{1}{18}(x+3)^2(x-2)^3$$

26.

$$y = -\frac{1}{45}(x+5)(x+2)(x-3)^2$$

Write the quadratic equation (standard form) that has the given vertex and point on the graph.

27. vertex:  $(5, 12)$ ; point  $(7, 15)$ 

$$y = a(x-5)^2 + 12$$

$$15 = a(7-5)^2 + 12$$

$$3 = a \cdot 4$$

$$\frac{3}{4} = a$$

$$y = \frac{3}{4}(x-5)^2 + 12$$

29. vertex:  $(-1, 4)$ ; point  $(-3, 0)$ 

$$y = a(x+1)^2 + 4$$

$$0 = a(-3+1)^2 + 4$$

$$-4 = a \cdot 4$$

$$\frac{-4}{4} = a = -1$$

$$y = -(x+1)^2 + 4$$

28. vertex:  $(-2, -2)$ ; point  $(-1, 0)$ 

$$y = a(x+2)^2 - 2$$

$$0 = a(-1+2)^2 - 2$$

$$2 = a \cdot 1$$

$$2 = a$$

$$y = 2(x+2)^2 - 2$$

30. vertex:  $(2, 3)$ ; point  $(0, 2)$ 

$$y = a(x-2)^2 + 3$$

$$2 = a(0-2)^2 + 3$$

$$-1 = a(4)$$

$$\frac{-1}{4} = a$$

$$y = -\frac{1}{4}(x-2)^2 + 3$$

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