

Review for Test 12

A bag contains 8 red marbles, 6 blue marbles, and 4 yellow marbles. Two marbles are selected at random, without replacement. Find the probability of each of the following.

1. P(red, then yellow) $\frac{8}{18} \cdot \frac{4}{17} = \frac{16}{153}$

2. P(2 blue) $= \frac{6}{18} \cdot \frac{5}{17} = \frac{5}{51}$

3. P(2 red or 2 blue) $\frac{8}{18} \cdot \frac{7}{17} + \frac{6}{18} \cdot \frac{5}{17} = \frac{43}{153}$

4. P(1 red and 1 yellow, in either order) $\frac{8}{18} \cdot \frac{4}{17} + \frac{4}{18} \cdot \frac{8}{17} = \frac{32}{153}$

One card is pulled from a standard deck of 52 cards. Find the probability of the following.

5. P(a face card) $\frac{12}{52} = \frac{3}{13}$

6. P(a heart) $\frac{13}{52} = \frac{1}{4}$

7. P(a face card or a heart) $\frac{12}{52} + \frac{13}{52} - \frac{3}{52} = \frac{22}{52} = \frac{11}{26}$

8. P(the jack of hearts) $\frac{1}{52}$

Find the odds of an event happening, given the probability of the event.

9. $\frac{4}{7}$ (4:3)

10. $\frac{2}{15}$ (2:13)

Find the probability of an event happening, given the odds of the event.

11. 10:3 $\frac{10}{13}$

12. 7:8 $\frac{7}{15}$

Solve. Round to 3 decimal places.

$P(x) = {}_n C_x \cdot p^x \cdot (1-p)^{n-x}$

13. On any given day, the probability that the entire Watson family eats dinner together is 2/5. Find the probability that, during any 7-day period, the Watson's eat dinner together at least six times.

$P(6) + P(7) = {}_7 C_6 \cdot \left(\frac{2}{5}\right)^6 \cdot \left(\frac{3}{5}\right)^1 + {}_7 C_7 \cdot \left(\frac{2}{5}\right)^7 \cdot \left(\frac{3}{5}\right)^0 = .019$

14. Assume that you are taking about 10-question multiple choice test. If each question has four choices and you have to guess on each question, what is the probability of getting exactly 7 questions correct?

$P(7) = {}_{10} C_7 \cdot \left(\frac{1}{4}\right)^7 \cdot \left(\frac{3}{4}\right)^3 = .003$

15. Eight unbiased coins were tossed simultaneously. Find the probability of getting exactly 4 heads.

$P(4) = {}_8 C_4 \cdot \left(\frac{1}{2}\right)^4 \cdot \left(\frac{1}{2}\right)^4 = .273$

16. A carton of 12 eggs at the grocery store has a 0.03 chance of having a cracked egg in the carton. What is the probability that less than 3 eggs are cracked?

$P(0) + P(1) + P(2) = {}_{12} C_0 \cdot (.03)^0 \cdot (.97)^{12} + {}_{12} C_1 \cdot (.03)^1 \cdot (.97)^{11} + {}_{12} C_2 \cdot (.03)^2 \cdot (.97)^{10} = .995$

17. According to government data, the probability that a woman between the ages of 25 and 29 was never married is 40%. In a random survey of 10 women in this age group what is the probability that two or fewer were never married?

$P(0) + P(1) + P(2) = {}_{10} C_0 \cdot (.40)^0 \cdot (.60)^{10} + {}_{10} C_1 \cdot (.40)^1 \cdot (.60)^9 + {}_{10} C_2 \cdot (.40)^2 \cdot (.60)^8 = .167$

18. Five dice are rolled. What is the probability that three of them are 6?

$P(3) = {}_5 C_3 \cdot \left(\frac{1}{6}\right)^3 \cdot \left(\frac{5}{6}\right)^2 = .032$